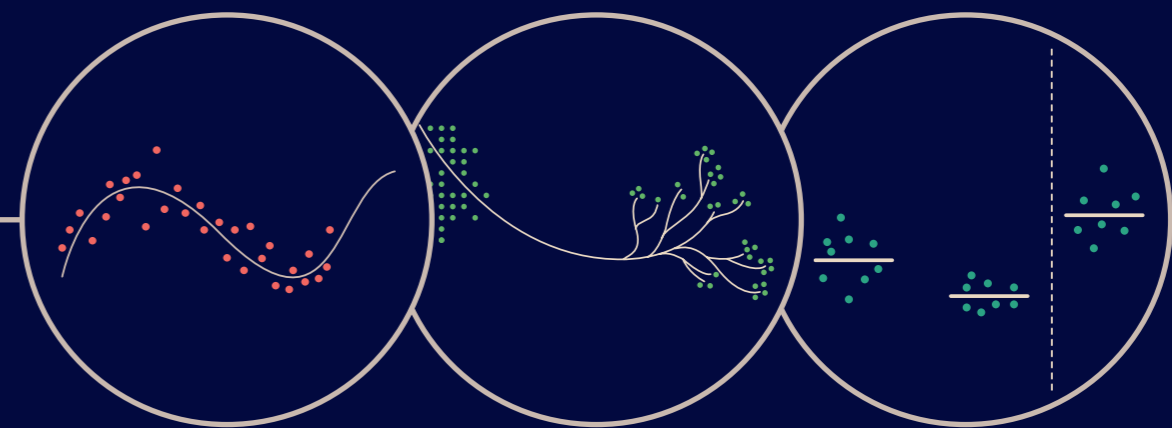


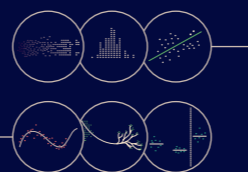
DATA ANALYSIS FOR BUSINESS, ECONOMICS, AND POLICY

Gábor Békés | Gábor Kézdi



Békés and Kézdi

DATA ANALYSIS
FOR BUSINESS,
ECONOMICS, AND POLICY



"This exciting new text covers everything today's aspiring data scientist needs to know, managing to be comprehensive as well as accessible. Like a good confidence interval, the Gabors have got you almost completely covered!"

Professor Joshua Angrist, Massachusetts Institute of Technology

"A beautiful integration of econometrics and data science that provides a direct path from data collection and exploratory analysis to conventional regression modeling, then on to prediction and causal modeling. Exactly what is needed to equip the next generation of students with the tools and insights from the two fields."

Professor David Card, University of California–Berkeley

"This textbook is excellent at dissecting and explaining the underlying process of data analysis. Békés and Kézdi have masterfully woven into their instruction a comprehensive range of case studies. The result is a rigorous textbook grounded in real-world learning, at once accessible and engaging to novice scholars and advanced practitioners alike. I have every confidence it will be valued by future generations."

Professor Kerwin K. Charles, Yale School of Management

This textbook provides future data analysts with the tools, methods, and skills needed to answer data-focused, real-life questions; to carry out data analysis; and to visualize and interpret results to support better decisions in business, economics, and public policy.

Data wrangling and exploration, regression analysis, machine learning, and causal analysis are comprehensively covered, as well as when, why, and how the methods work, and how they relate to each other.

As the most effective way to communicate data analysis, running case studies play a central role in this textbook. Each case starts with an industry-relevant question and answers it by using real-world data and applying the tools and methods covered in the textbook. Learning is then consolidated by 360 practice questions and 120 data exercises.

Extensive online resources, including raw and cleaned data and codes for all analysis in Stata, R, and Python, can be found at www.gabors-data-analysis.com.

Cover images: the cover illustrates steps and methods of data analysis. We reorganize messy into tidy datasets (L1), describe our data (C1), and estimate regression to uncover the patterns of association between variables (R1). To make predictions, we fit fluctuations in time series (L2) and use machine learning based on decision trees (C2). To learn the causal impact of interventions, we study events (R2). Cover illustration by Ágoston Nagy, 2019.

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Gábor Békés is an assistant professor at the Department of Economics and Business of the Central European University, and Director of the Business Analytics Program. He is a senior fellow at KRTK and a research affiliate at the Center for Economic Policy Research (CEPR). He has published in top economics journals on multinational firm activities and productivity, business clusters, and innovation spillovers. He has managed international data collection projects on firm performance and supply chains. He has done policy-advising (the European Commission, ECB) as well as private-sector consultancy (in finance, business intelligence, and real estate). He has taught graduate-level data analysis and economic geography courses since 2012.

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"This exciting new text covers everything today's aspiring data scientist needs to know, managing to be comprehensive as well as accessible. Like a good confidence interval, the Gabor's have got you almost completely covered!"

Professor Joshua Angrist, Massachusetts Institute of Technology

"This is an excellent book for students learning the art of modern data analytics. It combines the latest techniques with practical applications, replicating the implementation side of classroom teaching that is typically missing in textbooks. For example, they used the World Management Survey data to generate exercises on firm performance for students to gain experience in handling real data, with all its quirks, problems, and issues. For students looking to learn data analysis from one textbook, this is a great way to proceed."

Professor Nicholas Bloom, Department of Economics and Stanford Business School, Stanford University

"I know of few books about data analysis and visualization that are as comprehensive, deep, practical, and current as this one; and I know of almost none that are as fun to read. Gábor Békés and Gábor Kézdi have created a most unusual and most compelling beast: a textbook that teaches you the subject matter well and that, at the same time, you can enjoy reading cover to cover."

Professor Alberto Cairo, University of Miami

"A beautiful integration of econometrics and data science that provides a direct path from data collection and exploratory analysis to conventional regression modeling, then on to prediction and causal modeling. Exactly what is needed to equip the next generation of students with the tools and insights from the two fields."

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Professor Kerwin K. Charles, Yale School of Management

"This book takes you by the hand in a journey that will bring you to understand the core value of data in the fields of machine learning and economics. The large amount of accessible examples combined with the intuitive explanation of foundational concepts is an ideal mix for anyone who wants to do data analysis. It is highly recommended to anyone interested in the new way in which data will be analyzed in the social sciences in the next years."

Professor Christian Fons-Rosen, Barcelona Graduate School of Economics

"This sophisticatedly simple book is ideal for undergraduate- or Master's-level Data Analytics courses with a broad audience. The authors discuss the key aspects of examining data, regression analysis, prediction, Lasso, random forests, and more, using elegant prose instead of algebra. Using well-chosen case studies, they illustrate the techniques and discuss all of them patiently and thoroughly."

Professor Carter Hill, Louisiana State University

"This is not an econometrics textbook. It is a data analysis textbook. And a highly unusual one - written in plain English, based on simplified notation, and full of case studies. An excellent starting point for future data analysts or anyone interested in finding out what data can tell us."

Professor Beata Javorcik, University of Oxford

"A multifaceted book that considers many sides of data analysis, all of them important for the contemporary student and practitioner. It brings together classical statistics, regression, and causal inference, sending the message that awareness of all three aspects is important for success in this field. Many 'best practices' are discussed in accessible language, and illustrated using interesting datasets."

Professor Ilya Ryzhov, University of Maryland

"This is a fantastic book to have. Strong data skills are critical for modern business and economic research, and this text provides a thorough and practical guide to acquiring them. Highly recommended."

Professor John van Reenen, MIT Sloan

"Energy and climate change is a major public policy challenge, where high-quality data analysis is the foundation of solid policy. This textbook will make an important contribution to this with its innovative approach. In addition to the comprehensive treatment of modern econometric techniques, the book also covers the less glamorous but crucial aspects of procuring and cleaning data, and drawing useful inferences from less-than-perfect datasets. An important and practical combination for both academic and policy professionals."

Laszlo Varro, Chief Economist, International Energy Agency

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Central European University, Vienna and Budapest

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PROOF

WHY USE THIS BOOK

An applied data analysis textbook for future professionals

Data analysis is a process. It starts with formulating a question and collecting appropriate data, or assessing whether the available data can help answer the question. Then comes cleaning and organizing the data, tedious but essential tasks that affect the results of the analysis as much as any other step in the process. Exploratory data analysis gives context to the eventual results and helps deciding the details of the analytical method to be applied. The main analysis consists of choosing and implementing the method to answer the question, with potential robustness checks. Along the way, correct interpretation and effective presentation of the results are crucial. Carefully crafted data visualization help summarize our findings and convey key messages. The final task is to answer the original question, with potential qualifications and directions for future inquiries.

Our textbook **equips future data analysts with the most important tools, methods, and skills** they need through the entire process of data analysis to answer data focused, real-life questions. We cover all the fundamental methods that help along the process of data analysis. The textbook is divided into four parts covering **data wrangling and exploration, regression analysis, prediction with machine learning, and causal analysis**. We explain when, why, and how the various methods work, and how they are related to each other.

Our approach has a **different focus compared to the typical textbooks** in econometrics and data science. They are often excellent in teaching many econometric and machine learning methods. But they don't give much guidance about how to carry out an actual data analysis project from beginning to end. Instead, students have to learn all of that when they work through individual projects, guided by their teachers, advisors, and peers – but not their textbooks.

To cover all of the steps that are necessary to carry out an actual data analysis project, we **built a large number of fully developed case studies**. While each case study focuses on the particular method discussed in the chapter, they illustrate all elements of the process from question through analysis to conclusion. We facilitate individual work by **sharing all data and code in Stata, R, and Python**.

Curated content and focus for the modern data analyst

Our textbook focuses on the most relevant tools and methods. Instead of dumping many methods on the students, we selected the most widely used methods that tend to work well in many situations. That choice allowed us to discuss each method in detail so students can gain a deep understanding of when, why, and how those methods work. It also allows us to compare the different methods both in general and in the course of our case studies.

The textbook is divided into four parts. The first part starts with data collection and data quality, followed by organizing and cleaning data, **exploratory data analysis** and data visualization, generalizing from the data, and hypothesis testing. The second part gives a thorough introduction to **regression analysis**, including probability models and time series regressions. The third part covers **predictive analytics** and introduces cross-validation, LASSO, tree-based machine learning methods such as random forest, probability prediction, classification, and forecasting from time series data. The fourth part covers **causal analysis**, starting with the potential outcomes framework and causal maps, then discussing experiments, difference-in-differences analysis, various panel data methods, and the event study approach.

When deciding on which methods to discuss and in what depth, we drew on our own experience as well as the advice of many people. We have taught Data Analysis and Econometrics to students in Master's programs for years in Europe and the USA, and trained experts in business analytics, economics, and economic policy. We used earlier versions of this textbook in many courses with students who differed in background, interest, and career plans. In addition, we talked to many experts both in academia and in industry: teachers, researchers, analysts, and users of data analysis results. As a result, this textbook offers **a curated content that reflects the views of data analysts with a wide range of experiences.**

Real-life case studies in a central role

A cornerstone of this textbook are 43 case studies spreading over one-third of our material. This reflects our view that working through case studies is the best way to learn data analysis. Each of our case studies starts with a relevant question and answers it in the end, using real-life data and applying the tools and methods covered in the particular chapter.

Similarly to other textbooks, our case studies illustrate the methods covered in the textbook. In contrast with other textbooks, though, they are much more than that.

Each of our case studies is a fully developed story linking business or policy questions to decisions in data selection, application of methods and discussion of results. Each case study uses **real-life data** that is messy and often complicated, and it discusses data quality issues and the steps of data cleaning and organization along the way. Then, each case study includes **exploratory data analysis** to clarify the context and help choose the methods for the subsequent analysis. After carrying out the main **analysis**, each case study emphasizes the correct **interpretation** of the results, effective ways to present and visualize the results, and many include robustness checks. Finally, each case study **answers the question** it started with, usually with the necessary qualifications, discussing internal and external validity, and often raising additional questions and directions for further investigation.

Our case studies cover a wide range of topics, with a potential appeal to a wide range of students. They cover **consumer decision, economic and social policy, finance, business and management, health, and sport**. Their regional coverage is also wider than usual: one third are from the USA, one third are from Europe and the UK, and one third are from other countries or includes all countries from Australia to Thailand.

Support material with data and code shared

We offer a truly comprehensive material with data, code for all case studies, 360 **practice questions**, 120 **data exercises**, derivations for advanced materials, and reading suggestions. Each chapter ends with practice questions that help revise the material. They are followed by data exercises that invite students to carry out analysis on their own, in the form of robustness checks or replicating the analysis using other data.

We share all raw and cleaned data we use in the case studies. We also share the codes that clean the data and produce all results, tables, and graphs in **Stata, R, and Python** so students can tinker with our code and compare the solutions in the different software.

All data and code are available on the textbook website:

<http://gabors-data-analysis.com>

Who is this book for?

This textbook was written to be a **complete course** in data analysis. It introduces and discusses the most important concepts and methods in exploratory data analysis, regression analysis, machine learning and causal analysis. Thus, readers don't need to have a background in those areas.

The textbook includes formulae to define methods and tools, but it **explains all formulae in plain English**, both when a formula is introduced and, then, when it is used in a case study. Thus, understanding formulae is not necessary to learn data analysis from this textbook. They are of great help, though, and we encourage all students and practitioners to work with formulae whenever possible. The mathematics background required to understand these formulae is quite low, at the level of basic calculus.

This textbook could be useful for university students in graduate programs as **core text** in applied statistics and econometrics, quantitative methods, or data analysis. The textbook is best used as core text for non-research degree Masters programs or part of the curriculum in a PhD or research Masters programs. It may also **complement online courses** that teach specific methods to give more context and explanation. Undergraduate courses can also make use of this textbook, even though the workload on students exceeds the typical undergraduate workload. Finally, the textbook can serve as a **handbook for practitioners** to guide them through all steps of real-life data analysis.

SIMPLIFIED NOTATION

A note for the instructors who plan to use our textbook.

We introduced some new notation in this textbook, to make the formulae simpler and more focused. In particular, our **formula for regressions is slightly different** from the traditional formula. In line with other textbooks, we think that it is good practice to write out the formula for each regression that is analyzed. For this reason, it is important to use a notation for the regression formula that is as simple as possible and focuses only on what we care about. Our notation is intuitive, but it's slightly different from traditional practice. Let us explain our reasons.

Our approach starts with the definition of the regression: it is a model for the conditional mean. The formulaic definition of the simple linear regression is $E[y|x] = \alpha + \beta x$. The formulaic definition of a linear regression with three right-hand-side variables is $E[y|x_1, x_2, x_3] = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$.

The regression formula we use in the textbook is a simplified version of this formulaic definition. In particular, we have y^E on the left-hand side instead of $E[y|\dots]$. y^E is just a shorthand for the expected value of y conditional on whatever is on the right-hand side of the regression.

Thus, the formula for the simple linear regression is $y^E = \alpha + \beta x$, and y^E is the expected value of y conditional on x . The formula for the linear regression with three right-hand-side variables is $y^E = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$, and here y^E is the expected value of y conditional on x_1 , x_2 , and x_3 . Having y^E on the left-hand side makes notation much simpler than writing out the conditional expectation formula $E[y|\dots]$, especially when we have many right-hand-side variables.

In contrast, the traditional regression formula has the variable y itself on the left-hand side, not its conditional mean. Thus, it has to involve an additional element, the error term. For example, the traditional formula for the linear regression with three right-hand-side variables is $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + e$.

Our notation is simpler, because it has fewer elements. More importantly, our notation makes it explicit that the regression is a model for the conditional mean. It focuses on the data that analysts care about (the right-hand-side variables and their coefficients), without adding anything else.

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Creating the code base in Stata, R and Python was a massive endeavour. Both of us are primarily Stata users, and we needed R code that would be fairly consistent with Stata code. Plus, all graphs were produced in R. So we needed help to have all our Stata codes replicated in R, and a great deal of code writing from scratch. Zsuzsa Holler and Kinga Ritter have provided enormous development support, spearheading this effort for years. Additional code and refactoring in R was created by Máté Tóth, János Bíró, and Eszter Pázmándi. János and Máté also created the first version of Python notebooks. Additional coding, data collection, visualization, and editing were done by Viktória Kónya, Zsófia Kőműves, Dániel Bánki, Abuzar Ali, Endre Borza, Imola Csóka, and Ahmed Al Shaibani.

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